## Radical Goats

Juan wants to buy goats for his yard. He will build a pen to keep them safe. Each goat needs a certain amount of grazing area, so Juan will have to do some careful planning. Based on his research, he thinks that his pen should have a height that is two-thirds of the width. Let $w$ be the width of his pen and $A$ be the area of the pen.

1. Write a function of $A$ in terms of the width $w$.

2. Rewrite the function from (1) to be a function of $A$ in terms of $w$.
3. Graph the function from (2).
4. Juan wants to buy 15 goats. EACH goat needs a grazing area of $30-50$ square feet.
a. Based on these constraints, what is a reasonable domain restriction for the function from (2)?
b. What is the smallest width Juan's pen could have?
c. What is the largest width Juan's pen could have?

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5. Based on the cost of materials and feed, Juan decides his pen will have an area of 700 square feet. He will then hire a company to install the fence.
a. Create a sketch of the pen to give to the builders. Make sure to label all dimensions.
b. If the company charges $\$ 25$ per foot of fence installed, how much will Juan's pen cost?

Reflection: Is there a limit to how much area a goat should have? Discuss natural limits to this, thinking mathematically and reasonably. Why or why not?

