

August 20, 2018

Draw a supplementary angle

Draw a complementary angle

What do supplementary angles = ?

What do a complementary angles = ?

$$\text{complementary} = 90^\circ$$

$$\text{supplementary} = 180^\circ$$

Classify each angle as acute, obtuse, right, or straight.

1) obtuse

3) obtuse

5) acute

2) right

4) straight

6) acute

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$\angle$  = angle symbol

Name each angle in four ways.

7)  $\angle EDC$     8)  $\angle FGH$   
 $\angle CDE$      $\angle HGF$

9)  $\angle SD$     10)  $\angle JKL$   
 $\angle HGF$      $\angle TJK$   
 $\angle EGH$      $\angle LKJ$   
 $\angle G$      $\angle S$

Use the angle addition postulate to find the missing measurements.

11)  $m\angle HU = 152^\circ$  and  $m\angle HIF = 60^\circ$ . Find  $m\angle FIU$ .12)  $m\angle QRS = 135^\circ$  and  $m\angle QRH = 74^\circ$ . Find  $m\angle HRS$ .

Angle Addition Postulate

$$\begin{aligned} \angle HIF + \angle FIJ &= \angle HIJ \\ 60^\circ + x &= 152^\circ ? \\ -60^\circ &-60^\circ \\ x &= 92^\circ \end{aligned}$$

$$\begin{aligned} \angle SRH + \angle QRH &= \angle QRS \\ x + 74^\circ &= 135^\circ \\ -74^\circ &-74^\circ \\ x &= 61^\circ \end{aligned}$$

13) Find  $m\angle CDK$  if  $m\angle KDE = 160^\circ$  and  $m\angle CDE = 180^\circ$ .14)  $m\angle JKL = 107^\circ$  and  $m\angle MKL = 85^\circ$ . Find  $m\angle JKM$ .

$$\begin{aligned} \angle CDK + \angle KDE &= \angle CDE \\ x + 160^\circ &= 180^\circ \\ -160^\circ &-160^\circ \\ x &= 20^\circ \\ \angle OK &= 20^\circ \end{aligned}$$

$$\begin{aligned} \angle JKM + \angle MKL &= \angle JKL \\ x + 85^\circ &= 107^\circ \\ -85^\circ &-85^\circ \\ x &= 22^\circ \\ \angle JKM &= 22^\circ \end{aligned}$$

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15)  $m\angle FGZ = 52^\circ$  and  $m\angle ZGH = 94^\circ$ . Find  $m\angle PGH$ .

$\angle FGZ + \angle ZGH = \angle FGH$   
 $52^\circ + 94^\circ = x$   
 $146^\circ = x$

16) Find  $m\angle JIH$  if  $m\angle JIG = 70^\circ$  and  $m\angle GHJ = 52^\circ$ .

$\angle GIH + \angle JIG = \angle JIH$   
 $52^\circ + 70^\circ = x$   
 $122^\circ = x$   
 $122^\circ = \angle JIH$

or supplement

Name the relationship: complementary, linear pair, vertical, or adjacent.

17) linear pair

18) linear pair = Supplementary Angle  $\approx 180^\circ$

19) complementary

20) vertical

21) adjacent

22) complementary

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Using vertical pairs, find the measure of angle b.

23) Vertical angle  $b = 73^\circ$

24) Vertical angles are equal  $b = 52^\circ$

25) Vertical angle  $b = 59^\circ$

26) Vertical angle  $b = 35^\circ$

27)  $b + 64^\circ = 90^\circ$   
 $b = 26^\circ$

28) Complementary angle  $\angle b + 35^\circ = 90^\circ$   
 $b = 55^\circ$

Using complementary angles, find the value of x.

29)  $(5x+2)^\circ + 23^\circ = 90^\circ$   
 $5x + 28^\circ = 90^\circ$   
 $5x = 62^\circ$   
 $x = 13^\circ$

30)  $(x-9)^\circ + 57^\circ = 90^\circ$   
 $x - 57^\circ = 90^\circ$   
 $x = 147^\circ$

likewise  
 $x - 9 + 66^\circ = 90^\circ$   
 $x + 57^\circ = 90^\circ$   
 $x = 33^\circ$

31) Line  $x-3 + 2x = 90^\circ$   
 $3x - 3 = 90^\circ$   
 $3x = 93^\circ$   
 $x = 31^\circ$

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Using linear pairs, find the measure of angle b.

32)  $123^\circ + b = 180^\circ$   
 $b = 57^\circ$

33)  $61^\circ + b = 180^\circ$   
 $b = 119^\circ$

34)  $48^\circ + b = 180^\circ$   
 $b = 132^\circ$

Find the value of x.

35) Line  $(4x+3)^\circ + 77^\circ = 180^\circ$   
 $4x + 80^\circ = 180^\circ$   
 $4x = 100^\circ$   
 $x = 25^\circ$

36)  $(2x+9)^\circ + (3x+1)^\circ = 180^\circ$   
 $5x + 10^\circ = 180^\circ$   
 $5x = 170^\circ$   
 $x = 34^\circ$

37)  $(x+10)^\circ + (2x+1)^\circ = 180^\circ$   
 $3x + 11^\circ = 180^\circ$   
 $3x = 169^\circ$   
 $x = 56.3^\circ$

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Complementary Angles: Find the measure of angle b.

38)  $b = 67^\circ$

39)  $b = 38^\circ$

40)  $b = 63^\circ$

41)  $b = 41^\circ$

Supplementary Angles: Find the measure of angle b.

42)  $b = 150^\circ$

43)  $b = 29^\circ$

44)  $b = 138^\circ$

45)  $b = 92^\circ$

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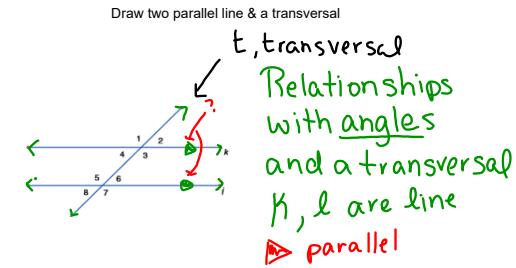
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August 21, 2018

Use tech:

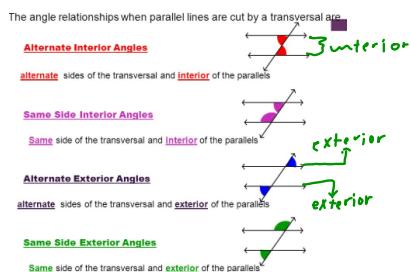
What is a transversal in mathematics?

Draw a picture.



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Write the angle relationship for each pair of angles.

Vocabulary:  
 - Alternate Interior Angles  
 - Alternate Exterior Angles  
 - Corresponding Angles  
 - Complementary Angles  
 - Supplementary Angles  
 - Vertical Angles

**Some side interior angle, same side exterior angle**

<1 and <2 are	corresponding Ls	Alternate interior angles are equal
<1 and <3 are	supplementary Ls	Alternate exterior angles are equal
<1 and <4 are	vertical Ls	Complementary angles
<2 and <5 are	alternate interior Ls	the same
<2 and <6 are	same side interior Ls	90°
<2 and <7 are	corresponding Ls	supplementary angles
<3 and <8 are	alternate exterior Ls	vertical angles
<3 and <7 are	same side exterior Ls	equal to 180°
<4 and <5 are	supplementary Ls	the same
<4 and <6 are	vertical Ls	90°
<4 and <8 are	corresponding Ls	supplementary angles
<5 and <6 are	same side exterior Ls	equal to 180°
<5 and <7 are	supplementary Ls	vertical angles

**Some side exterior angle, same side exterior angle**

1) and 4 are \_\_\_\_\_  
 2) and 3 are \_\_\_\_\_  
 3) and 4 are \_\_\_\_\_  
 4) and 5 are \_\_\_\_\_  
 5) and 6 are \_\_\_\_\_  
 6) and 7 are \_\_\_\_\_

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transversal practice

Find the measure of each angle indicated.

1)  $\text{Same side interior}$   $? + 130^\circ = 180^\circ$   $? = 50^\circ$   
 2)  $\text{alternate exterior Ls}$   $10^\circ$   $10^\circ$   $? = 110^\circ$   
 3)  $\text{same side interior}$   $? + 83^\circ = 180^\circ$   $? = 97^\circ$   
 4)  $\text{Vertical}$   $-4x + 8x + 12 + 6x$   $2x = 16$   $x = 8$   
 5)  $\text{interior alternate Ls}$   $110^\circ$   $? + 8^\circ + 17x$   $-8^\circ$   $102^\circ = 17x$   $17^\circ$   $b = x$

Solve for x.

6)  $7x + 8^\circ = 9x - 4^\circ$   
 $-9x + 8^\circ = -9x - 4^\circ$   
 $-2x = -12^\circ$   
 $x = 6^\circ$

Find the measure of the angle indicated in bold.  
 7)  $11x + 2^\circ = 12x - 6^\circ$   
 $11x + 2^\circ = 12x - 6^\circ$   
 $-1x + 2^\circ = -6^\circ$   
 $11x = 12x - 8^\circ$   
 $11x = 12x - 8^\circ$   
 $11x - 12x = -8^\circ$   
 $-x = -8^\circ$   
 $x = 8^\circ$

Find the measure of the indicated angle that makes lines u and v parallel.

8)  $\text{alternate ext. Ls}$   $11x + 5^\circ$   $20x = 19x + 5^\circ$   $x = 5^\circ$   
 9)  $\text{alternate interior Ls}$   $? = 133^\circ$   
 10)  $\text{corresponding Ls}$   $? = 97^\circ$

Find the value of x that makes lines u and v parallel.

11)  $\text{Alternate exterior Ls}$   $7x + 8^\circ = 8x + 8^\circ$   
 $-7x + 8^\circ = -7x + 8^\circ$   
 $8^\circ = x$  SG!  
 12)  $10x + 10^\circ = 110^\circ$   
 $10x = 100^\circ$   
 $x = 10^\circ$

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August 22, 2018

Solve for ALL angles on the parallel lines and the transversal, given that  $\angle 4 = 5x + 35$  and  $\angle 7 = 45^\circ$

$$\begin{aligned} \text{supplementary } & (5 + 5x + 35) = 80 \\ 80 + 5x &= 80 \\ -80 & \\ 5x &= 0 \\ x &= 0 \end{aligned}$$

$$\begin{aligned} 2x + 20 &= 2(0) + 20 = 20 \\ 2(20) + 20 &= 60 \\ 60 + 35 &= 95 \\ 2x - 10 &= 2x + 20 - 35 \\ -10 &= -15 \\ -10 &= -10 \end{aligned}$$

What is the value for  $x$  and what is the measure of the top, right angle?

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**Study Guide**

**Unit 2 5.4.1**

**Given:** Lines AB and CD are parallel. Another line EF cuts across the two parallel lines.

- The two angles that sit on opposite sides of a transversal, inside the parallel lines are called **alternate interior angles** and would be congruent.
- The two angles that sit on the same side of a transversal and in the same location are called **corresponding angles**. These angles are congruent.

3) Solve for  $x$  and  $y$ , then find angle L5

$$\begin{aligned} x &= 16 \\ y &= 31 \\ A &= 118 \end{aligned}$$

4) Find the measure of the alternate exterior angles in the diagram below

$$x = 5 \quad \text{Angle measure} = 100$$

5) Find the value of  $x$ .

$$\begin{aligned} 7x + 2 + 108 &= 180 \\ 7x + 110 &= 180 \\ -110 & \\ 7x &= 70 \\ x &= 10 \end{aligned}$$

Properties of Angles

$$\begin{aligned} 7x + 2 + 108 &= 180 \\ 7x + 110 &= 180 \\ -110 & \\ 7x &= 70 \\ x &= 10 \end{aligned}$$

6) Find the value of  $x$ .

$$\begin{aligned} 9x + y &= 10 \\ 9x + 1 &= 10 \\ 9x &= 9 \\ x &= 1 \end{aligned}$$

7) If two angles add to  $180^\circ$  degrees, they are called **supplementary angles**.  
8) Two adjacent angles whose sum add to  $180^\circ$  degrees are called **linear pair** angles.  
9) When two lines intersect, there are two pairs of opposite angles that are called **vertical angles**.

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45

10) The measure of angle A is  $45^\circ$ . Find the complementary angle,  $\angle B$ .

$$115 + x = 90$$

$$-115$$

$$-45$$

$$x = 45$$

11) The measure of an angle is  $35^\circ$ . Find the supplementary angle,  $\angle C$ .

$$35 + \angle C = 180$$

$$-35$$

$$\angle C = 145$$

$$m \angle C = 145$$

12) In the diagram below,  $\angle 1$  and  $\angle 2$  are a linear pair. The  $m\angle 1 = 2x$  and  $m\angle 2 = 3x - 10$ . Find the measure of each angle.

$$m \angle 1 = 2x, m \angle 2 = 3x - 10$$

For questions 13-15, use the diagram to tell whether the angles are vertical angles, a linear pair, or neither.

13)  $\angle 1$  and  $\angle 3$  \_\_\_\_\_  
 14)  $\angle 2$  and  $\angle 3$  \_\_\_\_\_  
 15)  $\angle 3$  and  $\angle 7$  \_\_\_\_\_

5 Bonus Points: Solve for ALL angles in the diagram below. Label all four angle measures.

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quiz

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Congruent triangles p 194

**Your Turn**

Determine whether the given triangles are congruent. Explain your reasoning.

4.

5.

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**Example 2** Find the value of the variable that results in congruent triangles.

**A**

Step 1 Identify corresponding angles.  
 $\angle M$  corresponds to  $\angle J$ , because they have the same measure and they are formed by congruent corresponding sides. Similarly,  $\angle N$  corresponds to  $\angle K$ . So,  $\angle P$  corresponds to  $\angle L$ .

**Evaluate: Homework and Practice**

1. Describe a sequence of rigid motions that maps  $\triangle MNP$  onto  $\triangle MQR$  to show that  $\triangle MNP \cong \triangle MQR$ .

For 2–5, determine whether the given triangles are congruent. Explain your reasoning.

2.

3.

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4.

Find the value of the variable that results in congruent triangles.

5.

6.

7.

8.

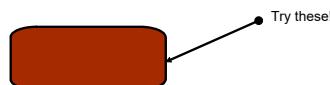
9.

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**Geogebra, interior triangle sum**

Be ready to share what you noticed....



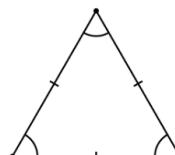
The Isosceles Triangle!

p 283, define isosceles triangle  
legs  
vertex angle  
base  
base angle

Be ready to label your vocabulary on this isosceles triangle!

**The equilateral triangle**

p 286 copy in your notebooks:  
**Equilateral Triangle Theorem**  
&  
**Converse of the Equilateral Triangle Theorem**

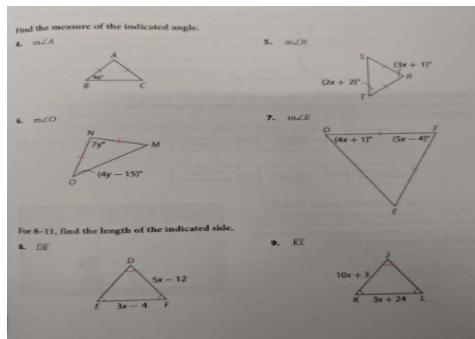


Be ready to explain the markings on this triangle!

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p289 - let's practice



Triangle Congruence..

What does congruence mean?

## The Rules

- p 203 copy ASA Triangle Congruence Theorem
- p 222 copy SSS Triangle Congruence Theorem
- p 227 copy AAS Triangle Congruence Theorem
- p 256 copy HL Triangle Congruence Theorem

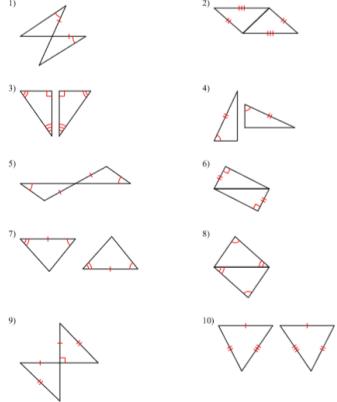
## The Practice

- p 206 #3-7
- p 227 #4-11
- p 250 #1-6
- p 258 #1-5

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State if the two triangles are congruent. If they are, state how you know.



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