

April 15, 2019, Monday

**Item 23**  
Selected-Response  
When rolling a number cube with sides numbered 1 through 6, what is the probability of rolling a number less than 3?

Handwritten:  $2, 4, 6 = 3$   
 $1 = \frac{1}{6}$

23 MGSE9-12.S.CP.7

The correct answer is choice (B)  $\frac{1}{3}$ . An even number or a number less than 3 includes the outcomes of 1, 2, 4, and 6, and there are 6 outcomes in the sample space;  $\frac{4}{6}$  simplifies to  $\frac{2}{3}$ . Choice (A) is incorrect because the probability of rolling a 1 and the probability of rolling a number less than 3 were added together without subtracting the overlap. Choice (C) is incorrect because it is the probability of an even number only. Choice (D) is incorrect because it is the probability of a number less than 3 only.

**Item 24**  
Selected-Response  
What is the probability of having an even number when you roll a 6-sided die?

Handwritten:  $\frac{4}{6}$

24 MGSE9-12.S.CP.3 2 B

The correct answer is choice (B)  $\frac{1}{2}$ . With the conditional probability, we assume that an odd number was rolled, which reduces our sample space to 1, 3, and 5. Out of those possibilities, the probability of rolling a 5 is  $\frac{1}{3}$ . 1 successful outcome out of 3 total outcomes. Choice (A) is incorrect because it is the probability of rolling a 5 without knowing an odd number was rolled. Choice (C) is incorrect because it is the probability of rolling an odd number. Choice (D) is incorrect because it is the complement of the correct answer.

**PARTS OF A CIRCLE**

EQ: What is a circle and how do we identify points, segments and lines that are related to a circle?

> A **circle** is a set of points in a plane that have an equal distance from a given point.

Read each of the questions below. How can you respond to the questions using one of the mentioned circle parts and the given visual?

- > The **Center** of a circle is a point that has an equal distance from each point on the circle. Which mentioned part is the center? **A**
- > A **radius** of a circle is a segment between the center and a point on the circle. Which mentioned part is a radius? **AB**
- > A **diameter** of a circle is a segment between two points on the circle whose midpoint is the center. Which mentioned part is a diameter? **CB**
- > A **chord** of a circle is a segment between two points on the circle. Which mentioned part is a non-diameter chord? **EF**
- > A **tangent** of a circle is a line that touches or intersects the circle at exactly one point. Which mentioned part is a tangent? **GH**
- > A **secant** of a circle is a line that touches or intersects the circle at exactly two points. Which mentioned part is a secant? **JK**
- > The **Point of Tangency** of a circle is the point of intersection of a tangent and the circle. Which mentioned part is a point of tangency? **L**
- > How many radii make up a diameter? **2** How much of the diameter makes up a radius? **1/2**
- > From #2, segment AD is the mentioned radius. What are two other radii shown on the circle? **AC, AB**
- > From #4, segment EF is the mentioned non-diameter chord. What is another non-chord shown on the circle? **GH**

**TANGENT PROPERTY**  
On  $\overline{OT}$ , draw radius  $\overline{TN}$ . The tangent line is **perpendicular** to the radius drawn to the tangent point.

**Pythagorean Theorem**  
 $a^2 + b^2 = c^2$

For #1-6, ✓ whether the line or segment is best described as a radius, diameter, chord, secant or tangent.

	Radius	Diameter	Chord	Secant	Tangent
1. $\overline{AD}$		✓			
2. $\overline{CD}$	✓				
3. $\overline{EG}$			✓		
4. $\overline{HB}$				✓	
5. $\overline{IB}$					✓
6. $\overline{AD}$					✓

For #7-12, ✓ whether the line or segment is best described as a radius, diameter, chord, secant or tangent.

	Radius	Diameter	Chord	Secant	Tangent
7. $\overline{AE}$				✓	
8. $\overline{BD}$					✓
9. $\overline{AB}$		✓			
10. $\overline{AB}$			✓		
11. $\overline{EA}$					✓
12. $\overline{BC}$					✓

For #13-16, write whether  $\overline{AB}$  is tangent to  $\odot O$  or not. Show work.

13. **Pythagorean Theorem works, yes it is a point of tangency.**  
 $9^2 + 12^2 = 14^2$   
 $81 + 144 = 196$   
 $225 \neq 196$

14.  $9^2 + 12^2 = 14^2$   
 $81 + 144 = 196$   
 $225 \neq 196$

15.  $7.5^2 + 10^2 = 12.5^2$   
 $56.25 + 100 = 156.25$   
 $156.25 = 156.25$

16.  $5^2 + 12^2 = 13^2$   
 $25 + 144 = 169$   
 $169 = 169$

**RELATIONSHIPS BETWEEN TWO CIRCLES**

No Points of Intersection: Three circles do not intersect. These are **CONCENTRIC CIRCLES** because they have the same center.

1 Point of Intersection: These are **INTERNALLY TANGENT CIRCLES** because one is inside the other.

2 Points: These circles intersect at a maximum of 2 points. These are **EXTERNALLY TANGENT CIRCLES** because one is outside the other.

**COMMON TANGENTS BETWEEN TWO CIRCLES**

These are **COMMON INTERNAL TANGENTS** because they intersect the segment that joins the centers of the two circles.

These are **COMMON EXTERNAL TANGENTS** because they do not intersect the segment that joins the centers of the two circles.

For #17-24, match the notation with the term that best describes it.

17. F	A. Center
18. $\overline{GD}$	B. Chord
19. HC	C. Diameter
20. DB	D. Radius
21. C	E. Tangent Point
22. BE	F. Common External Tangent
23. $\overline{EB}$	G. Common Internal Tangent
24. $\overline{AE}$	H. Secant

**SEGMENTS** are segments on tangents that are congruent.

How do we know tangent segments are congruent?

What kinds of circle parts are line AB and line CD? **tangent**  
What kind of angles are  $\angle TAB$  and  $\angle TCB$ ? **right angles**  
TB is TB. What part of the right triangle is TB to  $\triangle TAB$  and  $\triangle TCB$ ? **hypotenuse**  
TA is TC. What kinds of circle parts are TA and TC to  $\odot O$ ? **radii**  
What part of the right triangle is TA to  $\triangle TAB$  and TC to  $\triangle TCB$ ? **legs**  
WHY are AB congruent to CB? **congruent**. AB is CB because CPCTC.

For each of the following, find the unknown tangent segments by using the process we used to find the requested measures?

25.  $3x - 9 = 2x + 16$   
 $3x - 2x = 16 + 9$   
 $x = 25$   
 $AB = 12$ ,  $QC = 5$ ,  $QB = 13$ ,  $x = 7$ ,  $CB = 15$ ,  $QA = 8$ ,  $QB = 17$

26.  $2x + 1 = 3x - 6$   
 $2x - 3x = -6 - 1$   
 $-x = -7$   
 $x = 7$

How can we show the process for finding the perimeter of each quadrilateral?

27.	28.	29.	30.
Perimeter of Quadrilateral NWAK =	Perimeter of Quadrilateral PIVE =	Perimeter of Quadrilateral ALSV =	Perimeter of Quadrilateral LSFE =

**ARC AND CENTRAL ANGLES OF A CIRCLE**

EQ: What is the relationship between major arcs, minor arcs and central angles of a circle?

> An **arc** is a continuous part of a circle. There are several arcs and angles of a circle that are of interest to us. In the given circle below, some of these parts are  $\angle DBE$ ,  $\overline{DE}$ ,  $\overline{DB}$ ,  $\overline{BE}$ ,  $\overline{AC}$  and  $\overline{BC}$ .

Read each of the questions below. How can you respond to the questions using the mentioned circle parts and the given visual?

- > **Central angle** of a circle is an angle whose vertex is the center of the circle and whose sides are radii of the circle. Which mentioned part is a central angle?  **$\angle DBE$**
- > A **minor arc** is part of a circle that measures less than  $180^\circ$ . Which two mentioned parts are **minor arcs**? **AC**
- > A **semicircle** is an arc of a circle that equals  $180^\circ$ . Which mentioned part is a **semicircle**? **arc DEC**
- > A **major arc** is part of a circle that measures more than  $180^\circ$ . Which mentioned part is a **major arc**? **arc ACE**
- > **congruent** are two or more things that have the same measure. Which pair of mentioned parts are **congruent arcs**? **AD, AC**










EX: How can we check whether the given arc is a minor arc, major arc or semicircle of  $\odot O$ ?









Given Arc	Minor Arc	Major Arc	Semicircle
1. $\overline{AE}$	✓		
2. $\overline{EB}$		✓	
3. $\overline{FE}$			✓
4. $\overline{FB}$	✓		
5. $\overline{BF}$		✓	
6. $\overline{FB}$			✓

How many degrees is a circle? **360** How many degrees is a semicircle? **180** How can we use this information to help us find the measure of each arc?

Example: Find the measure of the given arcs.

1. $m\overline{QR}$	<b>70</b>
2. $m\overline{RQ}$	<b>180</b>
3. $m\overline{ER}$	<b>110</b>
4. $m\overline{SR}$	<b>110 + 70 + 30 = 210</b>
5. $m\overline{SP}$	<b>80</b>
6. $m\overline{RQ}$	<b>80</b>
7. $m\overline{PR}$	<b>80</b>
8. $m\overline{QR}$	<b>80</b>

<p><b>OUR TURN</b></p> <p>1. </p> <p><math>m\widehat{AN} = \dots</math>   <math>m\widehat{BN} = \dots</math>   <math>m\widehat{CN} = \dots</math>   <math>m\widehat{DEP} = \dots</math></p> <p><math>m\widehat{FAD} = \dots</math>   <math>m\widehat{GEP} = \dots</math>   <math>m\widehat{HFP} = \dots</math></p> <p>5. </p> <p><math>m\widehat{CD} = \dots</math>   <math>m\widehat{BE} = \dots</math>   <math>m\widehat{DEB} = \dots</math>   <math>m\widehat{DEC} = \dots</math></p> <p>8. </p> <p><math>m\widehat{BE} = \dots</math>   <math>m\widehat{AB} = \dots</math>   <math>m\widehat{AEB} = \dots</math>   <math>m\widehat{ABE} = \dots</math></p> <p>7. </p> <p><math>m\widehat{FT} = \dots</math>   <math>m\widehat{RHT} = \dots</math>   <math>m\widehat{RFT} = \dots</math>   <math>m\widehat{TRF} = \dots</math></p> <p>9. </p> <p><math>m\widehat{NM} = \dots</math>   <math>m\widehat{MP} = \dots</math>   <math>m\widehat{NDP} = \dots</math>   <math>m\widehat{NMP} = \dots</math></p>	<p><b>YOUR TURN</b></p> <p>2. </p> <p>4. </p> <p>6. </p> <p>10. </p>
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<p>11. </p> <p><math>m\widehat{QR} = \dots</math>   <math>m\widehat{RN} = \dots</math>   <math>m\widehat{QRN} = \dots</math>   <math>m\widehat{QRN} = \dots</math></p> <p><math>m\widehat{QRM} = \dots</math>   <math>m\widehat{NQM} = \dots</math>   <math>m\widehat{QRM} = \dots</math>   <math>m\widehat{NQM} = \dots</math></p> <p>13. </p> <p><math>m\widehat{HJ} = \dots</math>   <math>m\widehat{LKH} = \dots</math>   <math>m\widehat{HJL} = \dots</math>   <math>m\widehat{LKH} = \dots</math></p> <p><math>m\widehat{KLJ} = \dots</math>   <math>m\widehat{HLJ} = \dots</math>   <math>m\widehat{KLJ} = \dots</math>   <math>m\widehat{HLJ} = \dots</math></p> <p>15. </p> <p><math>m\widehat{AC} = \dots</math>   <math>m\widehat{CB} = \dots</math>   <math>m\widehat{ACB} = \dots</math>   <math>m\widehat{CBA} = \dots</math></p> <p><math>m\widehat{BAC} = \dots</math>   <math>m\widehat{CBA} = \dots</math>   <math>m\widehat{BAC} = \dots</math>   <math>m\widehat{CBA} = \dots</math></p> <p>17. </p> <p><math>m\widehat{QR} = \dots</math>   <math>m\widehat{RS} = \dots</math>   <math>m\widehat{QR} = \dots</math>   <math>m\widehat{RS} = \dots</math></p> <p><math>m\widehat{ST} = \dots</math>   <math>m\widehat{TQ} = \dots</math>   <math>m\widehat{ST} = \dots</math>   <math>m\widehat{TQ} = \dots</math></p>	<p>12. </p> <p>14. </p> <p>16. </p> <p>18. </p>
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April 16, 2019, Tuesday

**Item 22**

Constructed Response

There are 52 cards in a deck. Each card in the deck is numbered with the whole numbers 1 through 13. Each number appears on 4 cards in the deck. A student draws a card from the deck and then draws another card without replacing the first.

**Part A** What is the probability of picking a 1 on the first draw and then a 7 on the second draw? Write your answer in the space provided.

**Part B** Explain why picking a 1 first and a 7 second are NOT independent events. Write your answer in the space provided.

Part A \_\_\_\_\_

Part B \_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

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

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

Points Awarded
2
1
0

**INSCRIBED ANGLES OF A CIRCLE**





Analyze the angles in Circle O below. Distinguish between the two.





<p><b>CENTRAL <math>\angle ACB</math></b></p> <p>The central angle has the <math>60^\circ</math> arc as its vertex and <math>C</math> as its sides.</p> 	<p><b>INSCRIBED <math>\angle APB</math></b></p> <p>The inscribed angle has a <math>60^\circ</math> arc on the circle as its vertex and <math>P</math> as its sides.</p> 
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**Formulas**







<p><b>Central Angle</b></p> <p>Vertex is in center of circle</p>  <p><math>m\angle CAD = m\widehat{CD}</math></p>	<p><b>INSCRIBED ANGLE</b></p> <p>Vertex is on circle</p>  <p><math>m\angle CAD = \frac{1}{2}(m\widehat{CD})</math></p>
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For #1-8, find the measure of the arc, central angle and inscribed angle.





1 	2 	3 	4 
ARC $\widehat{AB}$ _____	ARC $\widehat{AB}$ _____	ARC $\widehat{AB}$ _____	ARC $\widehat{AB}$ _____
CENTRAL $\angle ACB$ _____	CENTRAL $\angle ACB$ _____	CENTRAL $\angle ACB$ _____	CENTRAL $\angle ACB$ _____
INSCRIBED $\angle APB$ _____	INSCRIBED $\angle APB$ _____	INSCRIBED $\angle APB$ _____	INSCRIBED $\angle APB$ _____

5 	6 	7 	8 
ARC $\widehat{AB}$ _____	ARC $\widehat{AB}$ _____	ARC $\widehat{AB}$ _____	ARC $\widehat{AB}$ _____
CENTRAL $\angle ACB$ _____	CENTRAL $\angle ACB$ _____	CENTRAL $\angle ACB$ _____	CENTRAL $\angle ACB$ _____
INSCRIBED $\angle APB$ _____	INSCRIBED $\angle APB$ _____	INSCRIBED $\angle APB$ _____	INSCRIBED $\angle APB$ _____



For #9-14, find the measure of the requested angle or arc.



9 	10 	11 
$m\angle NGL = \dots$	$m\angle KND = \dots$	$m\angle TXR = \dots$
12 	13 	14 
$m\widehat{BR} = \dots$	$m\widehat{SE} = \dots$	$m\widehat{WZ} = \dots$

For #15-26, find the measure of the requested angle or arc.



<p><b>15</b> </p> <p><math>m\angle ER = \dots</math></p> <p><math>m\angle TC = \dots</math></p> <p><math>m\angle TLR = \dots</math></p> <p><math>m\angle LRT = \dots</math></p> <p><b>17</b> </p> <p><math>m\angle EM = \dots</math></p> <p><math>m\angle MEC = \dots</math></p> <p><math>m\angle MOD = \dots</math></p> <p><math>m\angle MLD = \dots</math></p>	<p><b>16</b> </p> <p><math>m\angle QZ = \dots</math></p> <p><math>m\angle QIX = \dots</math></p> <p><math>m\angle QXX = \dots</math></p> <p><b>18</b> </p> <p><math>m\angle EB = \dots</math></p> <p><math>m\angle EB = \dots</math></p> <p><math>m\angle COL = \dots</math></p> <p><math>m\angle CSL = \dots</math></p>
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**INSCRIBED QUADRILATERALS**



<p><b>19</b> </p> <p><math>m\angle DTL = \dots</math></p> <p><math>m\angle QLE = \dots</math></p> <p><math>m\angle QDT = \dots</math></p> <p><math>m\angle QLT = \dots</math></p>	<p><b>20</b> </p> <p><math>m\angle KYZ = \dots</math></p> <p><math>m\angle WYZ = \dots</math></p> <p><math>m\angle WKT = \dots</math></p> <p><math>m\angle QLT = \dots</math></p>
--	--

<p><b>23</b> </p> <p><math>m\widehat{CR} = \dots</math></p> <p><math>m\angle CDR = \dots</math></p> <p><math>m\widehat{RD} = \dots</math></p> <p><math>m\angle PCB = \dots</math></p> <p><math>m\widehat{PB} = \dots</math></p> <p><math>m\angle PFB = \dots</math></p> <p><math>m\widehat{BR} = \dots</math></p>	<p><b>24</b> </p> <p><math>m\angle T = \dots</math></p> <p><math>m\angle S = \dots</math></p> <p><math>m\angle T = \dots</math></p> <p><math>m\angle S = \dots</math></p>
--	--

**SOLVING EQUATIONS: For #25-26, solve for x and find each angle or arc. Show work.**

<p><b>25</b> </p> <p>Equation _____</p> <p><math>X = \dots</math></p> <p><math>m\widehat{SE} = \dots</math></p> <p><math>m\angle SCB = \dots</math></p> <p><math>m\angle CDB = \dots</math></p>	<p><b>26</b> </p> <p>Equation _____</p> <p><math>X = \dots</math></p> <p><math>m\angle REE = \dots</math></p> <p><math>m\angle CDB = \dots</math></p>
--	--

\* NOTE: For #27-28, inscribed angles with the same arc are congruent.

<p><b>27</b> </p> <p>Equation _____</p> <p><math>X = \dots</math></p> <p><math>m\angle ZHS = \dots</math></p> <p><math>m\angle ZFS = \dots</math></p> <p><math>m\angle ZS = \dots</math></p>	<p><b>28</b> </p> <p>Equation _____</p> <p><math>X = \dots</math></p> <p><math>m\angle CNT = \dots</math></p> <p><math>m\angle TGC = \dots</math></p> <p><math>m\angle CT = \dots</math></p>
---	---

NOTE: For #29-34, inscribed angles are formed by a tangent and a chord. Find the measure of each angle or arc.

29		30		31	
$m\angle PQR = \text{?}$	$m\angle PQR = \text{?}$	$m\angle PQR = \text{?}$	$m\angle PQR = \text{?}$	$m\angle PQR = \text{?}$	$m\angle PQR = \text{?}$
$m\text{Arc} PQR = \text{?}$	$m\text{Arc} PQR = \text{?}$	$m\text{Arc} PQR = \text{?}$	$m\text{Arc} PQR = \text{?}$	$m\text{Arc} PQR = \text{?}$	$m\text{Arc} PQR = \text{?}$

PARALLEL LINES

For #35-38, find the measure of each angle or arc.

35		36	
$m\angle PQR = \text{?}$	$m\angle PQR = \text{?}$	$m\angle PQR = \text{?}$	$m\angle PQR = \text{?}$
$m\text{Arc} PQR = \text{?}$	$m\text{Arc} PQR = \text{?}$	$m\text{Arc} PQR = \text{?}$	$m\text{Arc} PQR = \text{?}$

37		38	
$m\angle PQR = \text{?}$	$m\angle PQR = \text{?}$	$m\angle PQR = \text{?}$	$m\angle PQR = \text{?}$
$m\text{Arc} PQR = \text{?}$	$m\text{Arc} PQR = \text{?}$	$m\text{Arc} PQR = \text{?}$	$m\text{Arc} PQR = \text{?}$

Geometry - U4 Day 2  
 TOTD - Tangents, Central Angles, & Arcs

Name \_\_\_\_\_

Solve for x. Assume that lines which appear to be tangent are tangent.

1)

2)

Find the segment length indicated. Assume that lines which appear to be tangent are tangent.

3)

4)

Find the measure of the arc or central angle indicated. Assume that lines which appear to be diameters are actual diameters.

5)  $m\angle EFG = \text{?}$

6)  $m\text{Arc} MN = \text{?}$

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Solve for x. Assume that lines which appear to be diameters are actual diameters.

7)

8)

Find the measure of the arc or central angle indicated. Assume that lines which appear to be diameters are actual diameters.

9)  $m\angle EIJ = \text{?}$

10)  $m\text{Arc} EF = \text{?}$

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April 17, 2019, Wednesday

Item 15  
 Selected-Response  
 Look at quadrilateral QRST.

What is the image of point R after a counterclockwise rotation of 270 degrees about the origin?

A. (6, -3)  
 B. (-3, 6)  
 C. (-6, 3)  
 D. (3, -6)

15

RELATED ANGLES FROM INSCRIBED ANGLES

For #1-10,  $x^\circ$  is formed by the intersection of two chords. Use an auxiliary line and inscribed angles to solve for x.

$$m\angle x = \frac{1}{2}(\text{Arc} + \text{Arc})$$

1.	2.
$m\angle A = \text{?}$	$m\angle A = \text{?}$
3.	4.
$m\angle A = \text{?}$	$m\angle A = \text{?}$
5.	6.
$m\angle A = \text{?}$	$m\angle A = \text{?}$
7.	8.
$m\angle A = \text{?}$	$m\angle A = \text{?}$
9.	10.
$m\angle A = \text{?}$	$m\angle A = \text{?}$

For #11-20,  $x^\circ$  is formed by the intersection of two secants or by the intersection of a secant and tangent. Use an auxiliary line and inscribed angles to solve for x.

$$m\angle x = \frac{1}{2}(\text{Big Arc} - \text{Small Arc})$$

11.	12.
$m\angle A = \text{?}$	$m\angle A = \text{?}$
13.	14.
$m\angle A = \text{?}$	$m\angle A = \text{?}$
15.	16.
$m\angle A = \text{?}$	$m\angle A = \text{?}$
17.	18.
$m\angle A = \text{?}$	$m\angle A = \text{?}$
19.	20.
$m\angle A = \text{?}$	$m\angle A = \text{?}$

April 18, 2019, Thursday

**Item 16**  
Selected Response  
Look at the square WXYZ on this coordinate plane.

**Item 17**  
Selected Response  
What are the coordinates of a point that lies along the directed line segment from Q(2, 5) to R(7, 12) and partitions the segment in the ratio of 3 to 2?

A. (3, 4.2)  
B. (4.5, 8.5)  
C. (5, 9.2)  
D. (5, 7)

Which measure is closest to the perimeter of square WXYZ?

A. 20 units  
B. 25.6 units  
C. 32 units  
D. 40.9 units

**ARC LENGTH AND SECTOR AREA OF CIRCLES**

Let  $\theta$  (theta) represent the central angle of a circle. The sector of a circle is the partial area of the circle that contains the central angle and its arc.

The arc length of a circle represents part of the circumference of the circle.

$$\text{Arc Length} = \frac{\theta^\circ}{360^\circ} \cdot 2\pi r$$

The area of the sector represents part of the area of the circle.

$$\text{Sector Area} = \frac{\theta^\circ}{360^\circ} \cdot \pi r^2$$

For #1-5, the central angle and either the radius are given. How do we show the process for finding the arc length and sector area of each shaded region using proper units?

	Arc Length	Sector Area
1		
2		
3		

For #4-9, find the requested measure. Make sure to use appropriate units.

4	What is the area of the shaded part of the circle? 	5	What is the arc length of the shaded part of the circle? 
6	What is the arc length of the shaded part of the circle? 	7	What is the area of the shaded part of the circle? 
8	What is the area of the shaded part of the circle? 	9	What is the arc length of the shaded part of the circle? 

For #10-17, find the requested measure. Make sure to use appropriate units.

10	Length of the arc AB = 38.33 in 	11	Length of the arc CD = 15.18 in 
----	-------------------------------------	----	-------------------------------------

12	Length of the arc CD = 16.33 in 	13	Length of the arc YZ = 37.42 cm 
14	Area = 284.96 cm <sup>2</sup> 	15	Area = 529.35 in <sup>2</sup> 
16	Area = 52.33 m <sup>2</sup> 	17	Area = 153.86 cm <sup>2</sup> 

Geometry Name \_\_\_\_\_ ID: 1  
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**Arc Length & Sector Area** Date \_\_\_\_\_ Period \_\_\_\_\_

Find the length of each arc. Round your answers to the nearest tenth.

1)	2)
3)	4)
5)	6)

A) 23.0 in B) 52.4 in  
C) 40.8 in D) 523.6 in

A) 18π ft B)  $\frac{5\pi}{2}$  ft  
C) π ft D) 20π ft

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Find the area of each sector. Round your answers to the nearest tenth.

7)	8)
9)	10)
11)	12)

A) 47.1 in<sup>2</sup> B) 137.8 m<sup>2</sup>  
C) 25.1 m<sup>2</sup> D) 1.2 in<sup>2</sup>

A)  $\frac{95\pi}{3}$  km<sup>2</sup> B) 900π km<sup>2</sup>  
C)  $\frac{5231\pi}{24}$  km<sup>2</sup> D)  $\frac{25\pi}{2}$  km<sup>2</sup>

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April 19, 2019, Friday

**Item 18**  
Selected-Response

What is the equation of the line that is perpendicular to  $y = \frac{1}{2}x - 6$  and passes through the point (6, 4)?

A.  $y = -\frac{1}{2}x + 1$   
 B.  $y = -\frac{1}{2}x + 7$   
 C.  $y = -2x - 8$   
 D.  $y = -2x + 16$

18	MSGE9-12.G.GPE.5
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**Item 19**  
Selected-Response

Study this equation of a circle.

$$x^2 - 6x + y^2 + 2y + 6 = 0$$

Which of these represents the center and radius of the circle?

A. center: (3, -1), radius: 4  
 B. center: (-3, 1), radius: 4  
 C. center: (3, -1), radius: 2  
 D. center: (-3, 1), radius: 2

19	MSGE9-12.G.GPE.1
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Name: \_\_\_\_\_ Date: \_\_\_\_\_

**Geometry GROUP WORK**  
CIRCLES

Show all work by writing on your diagram! Answers will not be scored without writing on diagrams. One paper from your group will be randomly chosen to be scored for your whole group grade.

<p>1) Find the value of <math>v</math>.</p>	<p>2) Find the value of <math>x</math>.</p>
<p>3) Find the value of <math>y</math> by finding as many other angles and arcs as possible.</p>	<p>4) Find the value of <math>w</math> by finding as many other angles and arcs as possible.</p>
<p>5) Find the value of <math>z</math> by finding as many other angles and arcs as possible.</p>	<p>6) If <math>m\widehat{AB} = 60^\circ</math> and radius is 8 cm:              a) What is the length of <math>\widehat{AB}</math>? Include units.              b) What is the area of the <math>60^\circ</math> sector? Include units</p>
<p>7) A square is inscribed in a circle as shown. If the radius of the circle is 6 in., find the area of the shaded region.</p>	

<p>8) For <math>\odot O</math>, <math>m\widehat{AB} = 100^\circ</math> and <math>m\widehat{CD} = 30^\circ</math>. Find <math>x</math> and <math>y</math>. Show work.</p>	<p>9) If length of <math>\widehat{AB}</math> is <math>10\pi</math> cm, what is the circumference of the circle? Show work.</p>
<p>10) <math>\triangle ABC</math> is inscribed with base <math>\widehat{AB}</math>. <math>m\angle BAC = 35^\circ</math> and <math>m\angle C = 160^\circ</math>. Find all angles and arcs.</p>	<p>11) Find <math>m\widehat{AM}</math></p>
<p>12) In <math>\odot O</math>, write all angles and arcs in the figure that can be found.</p>	<p>13) Find all angles and arcs in the circle below.</p>

